

# Wetting and adhesion on nano-patterned surfaces,

## How geometry couples to physics

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20th May 2009

1 Liquid drops

2 Solid clusters

3 Membranes and Filaments

4 Conclusion

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# Some examples



- Contact angle
- Lotus effect



# Young contact angle

## Surface/Interface free Energies

$$\mathcal{F} = \int_{VS} ds \gamma_{VS}(\theta) + \int_{SA} ds \gamma_{SA}(\theta) + \int_{AV} ds \gamma(\theta)$$

Assumptions:

- (i) flat substrate
- (ii) fixed total volume:

$$\mathcal{N} = \Omega^{-1} \int \int_A d^2\mathbf{r}$$

Equilibrium:

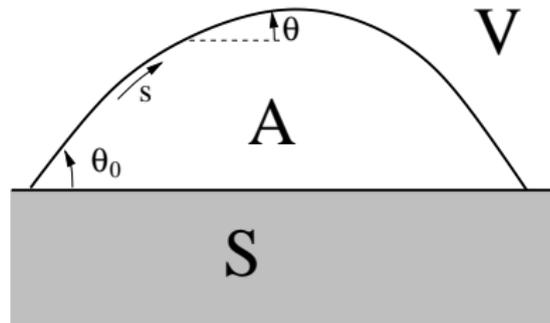
$$\delta(\mathcal{F} - \mu\mathcal{N}) = 0$$

Laplace:

$$\mu = \Omega \gamma_{AV} \kappa$$

Young relation (1805):

$$\gamma_{SA} + \gamma_{AV} \cos \theta_0 = \gamma_{SV}$$



# Super-hydro-phobic surfaces: Wenzel and Cassie-Baxter states

Bico, Marzolin, Quéré, Europhys. Lett (1999).

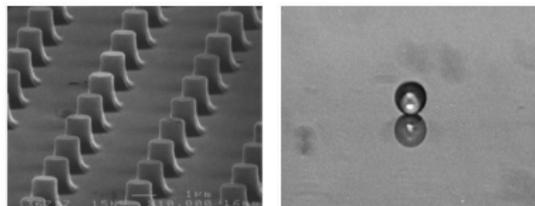
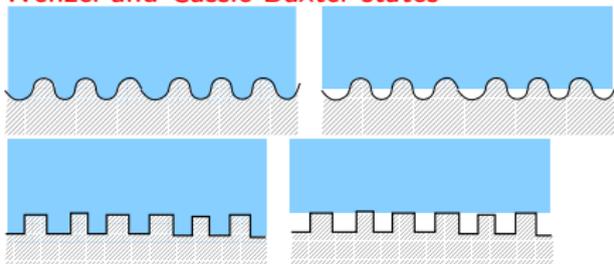


Figure 12. Substrate decorated with posts (the bar indicates 1 μm). If coated with a monolayer of fluorinated silanes, this substrate is found to be super-hydrophobic [37].

## Wenzel and Cassie-Baxter states



Effective contact angle:

$$\gamma_{SA}^{eff} + \gamma_{AV} \cos \theta_0 = \gamma_{SV}^{eff}$$

Wenzel (1936)

substrate lengthening  $r \geq 1$

$$\cos \theta_W = r \cos \theta_0$$

Cassie-Baxter (1944)

solid-liquid contact fraction  $\phi_{AS}$

liquid-vapor contact fraction  $\eta_{AV}$

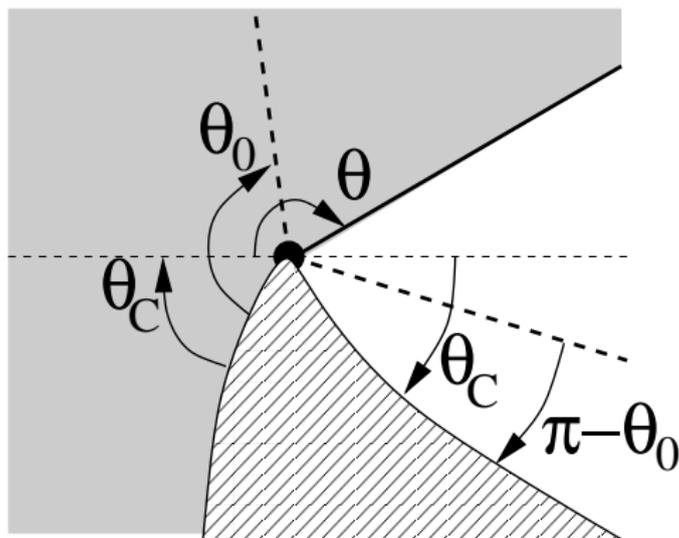
$$\cos \theta_{CB} = \phi_{AS} \cos \theta_0 - \eta_{AV}$$

## Pinning

Gibbs Inequality Condition (1906)

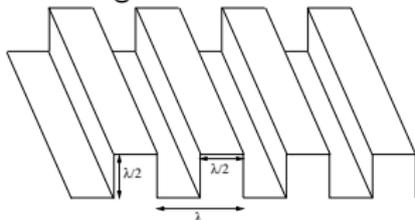
$$\theta_0 - \theta_C \leq \theta \leq \theta_0 + \theta_C$$

→ Pinning at corners

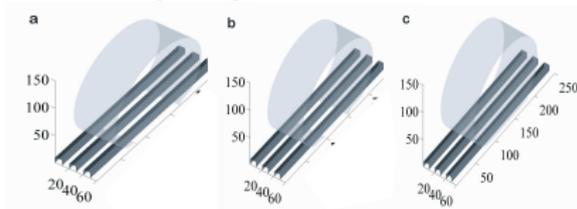


# Dynamics of lifting and collapse

Parallel grooves:



Lattice-Boltzmann simulations  
Solve the hydrodynamics

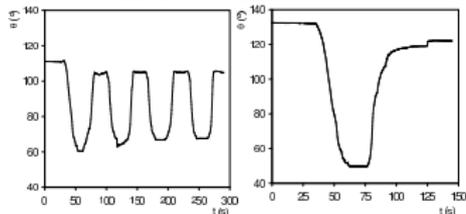
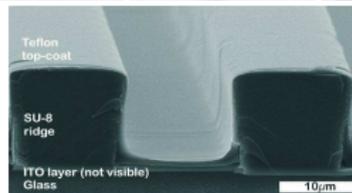


Movies

*R. J. Vrancken, H. Kusumaatmaja, K. Hermans, A.M. Preenen, O. Pierre Louis, C. W. M. Bastiaansen, D.J. Broer, preprint*

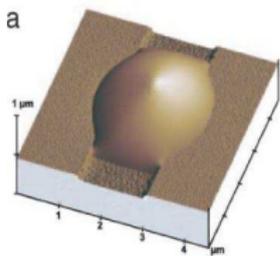
Electro-wetting experiments

Vary  $\theta_0$  continuously with  $V$

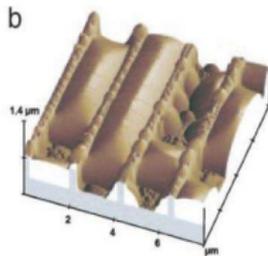


## Capillary filling

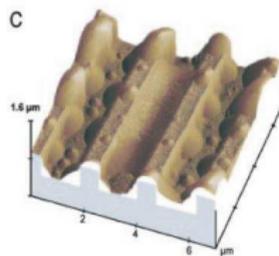
Seemanet *al* (2005)  
Polystyrene drops on Silicon



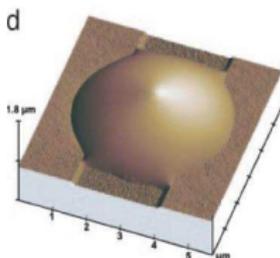
$$X = 0.063, \theta = 54 \pm 1$$



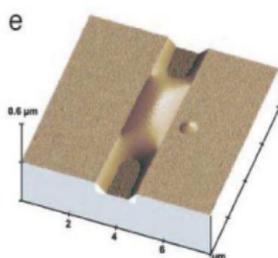
$$X = 0.405, \theta = 74 \pm 3$$



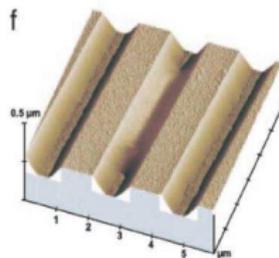
$$X = 0.49, \theta = 58 \pm 3$$



$$X = 0.031, \theta = 43 \pm 1$$



$$X = 0.063, \theta = 20 \pm 2$$



$$X = 0.165, \theta = 20 \pm 3$$

# Wetting of solid clusters on nano-patterned surfaces,

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1 Liquid drops

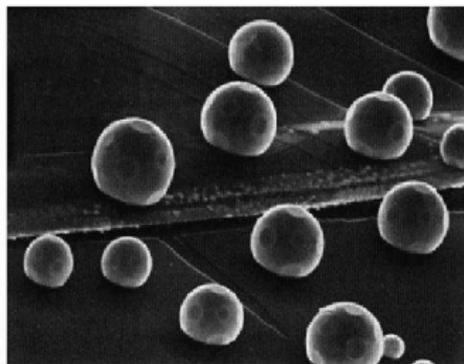
2 Solid clusters

3 Membranes and Filaments

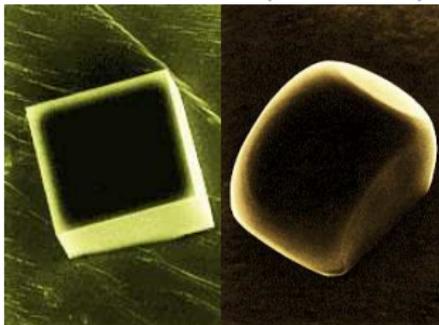
4 Conclusion

# Experimental equilibrium shape

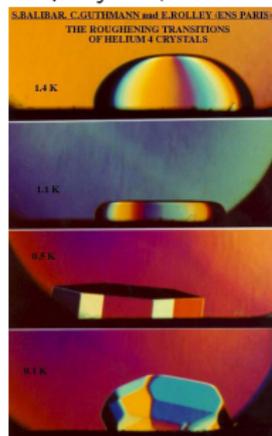
Au/Graphite, Héyraud, Métois, Marseille



NaCl, Métois et al (620-710°C)



He<sub>4</sub> crystal, Balibar et al, Paris



# Solids vs liquid

- Anisotropy: roughening transition  $\rightarrow$  facets

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- Energy: elasticity, electronic energy, etc.

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- Anisotropy: roughening transition  $\rightarrow$  facets
- Energy: elasticity, electronic energy, etc.
- Mass Transport: diffusion (surface atoms, or bulk vacancies)

# The Wulff and Kaishev constructions

Isotropic solid  $\gamma(\theta) = \bar{\gamma}$

$$\mu = \Omega \bar{\gamma} \kappa \Rightarrow R = \frac{\Omega \bar{\gamma}}{\mu}$$

$$\bar{\gamma} \cos(\theta_0) = -\gamma_S \Rightarrow h_s = \frac{\Omega \gamma_S}{\mu}$$

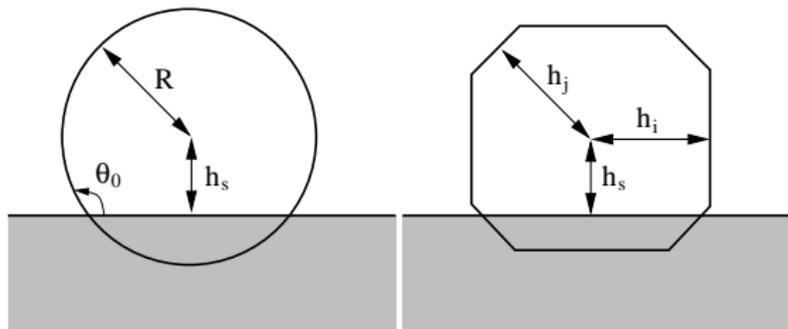
Polygonal shape

$$h_i = \frac{\Omega \gamma_i}{\mu}$$

$$h_s = \frac{\Omega \gamma_S}{\mu}$$

Global geometry

$$\psi = \frac{S_{AV}}{S_{AS}}$$



## 3D KMC Model

## 3D KMC

Hopping along the surface

$$\nu = \nu_0 e^{-(n_1 J_1 + n_2 J_2 + n_{s1} J_{s1} + n_{s2} J_{s2})/T}$$

$J$  bond energy,  $n_i$  nb neighbors

$i = 1$  NN adsorbate

$i = 2$  NNN adsorbate

$i = s1$  NN substrate

$i = s2$  NNN substrate

Moves to NN/ surface

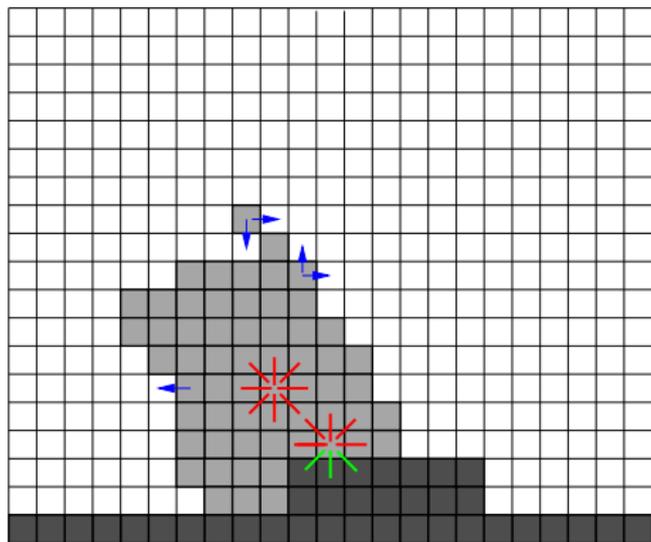
Shape parameter

$$\zeta = \frac{J_2}{J_1} = \frac{J_{s2}}{J_{s1}}$$

Wetting controlled by

$$\chi = \frac{J_{s1}}{J_1}$$

isotropic:  $\chi = (1 + \cos \theta_0)/2$

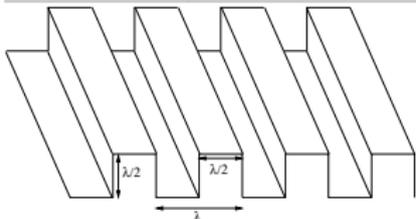
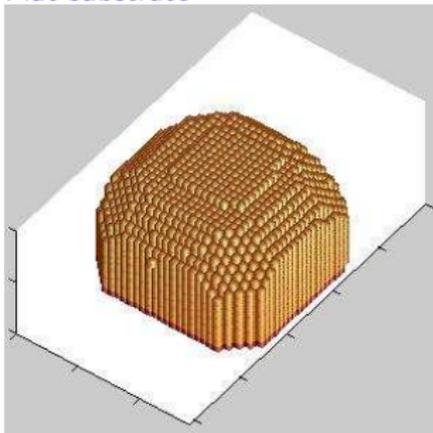


## Flat substrate vs parallel nanogrooves

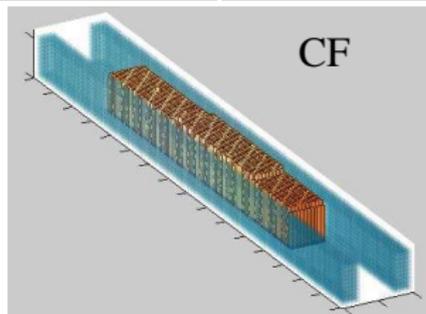
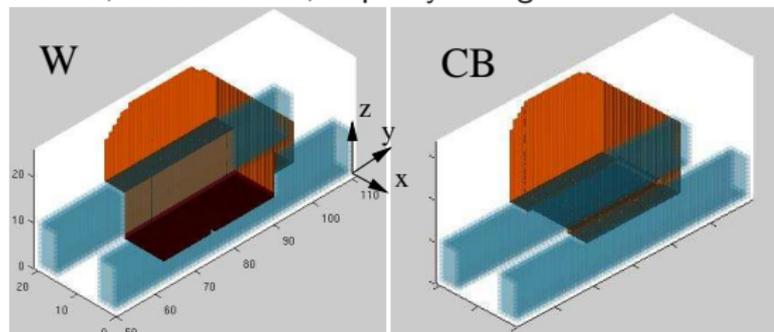
$$N = 10^4, \lambda = 20, \zeta = 0.2,$$

$$\chi = 0.4, T/J_1 = 0.5$$

Flat substrate

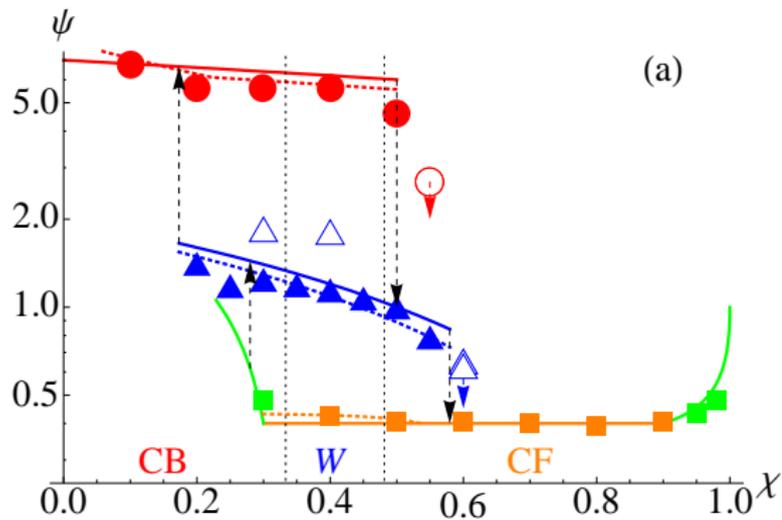
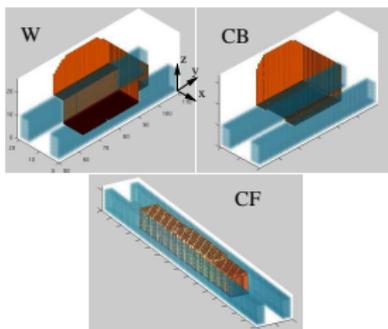


Parallel grooves  $\rightarrow$  3 states  
Wenzel, Cassie-Baxter, Capillary Filling



## Hysteresis

$$\psi = \frac{S_{AV}}{S_{AS}}, \quad \chi = \frac{J_{s1}}{J_1}$$



# Surface Diffusion

Mullins' Model

*Local* chemical potential  $\mu = \Omega\tilde{\gamma}\kappa$ .

Mullins model:

$$j = -\frac{Dc}{k_B T} \partial_s \mu$$

$$V_n = -\Omega \partial_s j$$

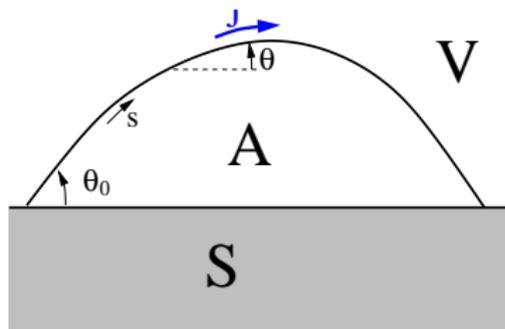
Triple Line

Equilibrium contact angle  $\theta = \theta_0$

Scaling

$$v_n \sim \partial_{ss} \kappa$$

Relaxation time  $t \sim L^4$



## Dynamics

## Dynamics limited by peeling or nucleation

Combe, Jensen, Pimpinelli, Phys Rev Lett 2000

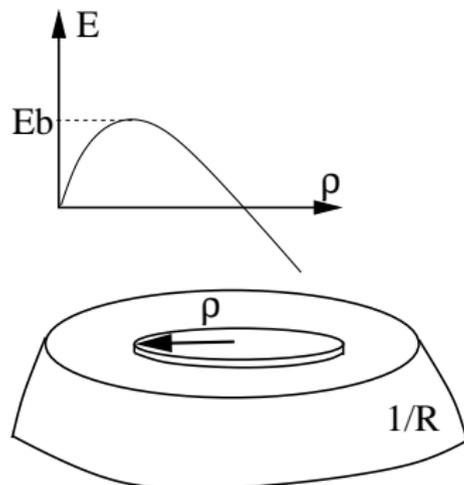
Mullins and Rohrer, J. Am. Ceram. Soc. 2000

Activation energy:  $\sim$  lateral size  $R$ Cost:  $\gamma_{step} 2\pi\rho$ Gain:  $\gamma_{rough}(1/R)$  per atom

Total:

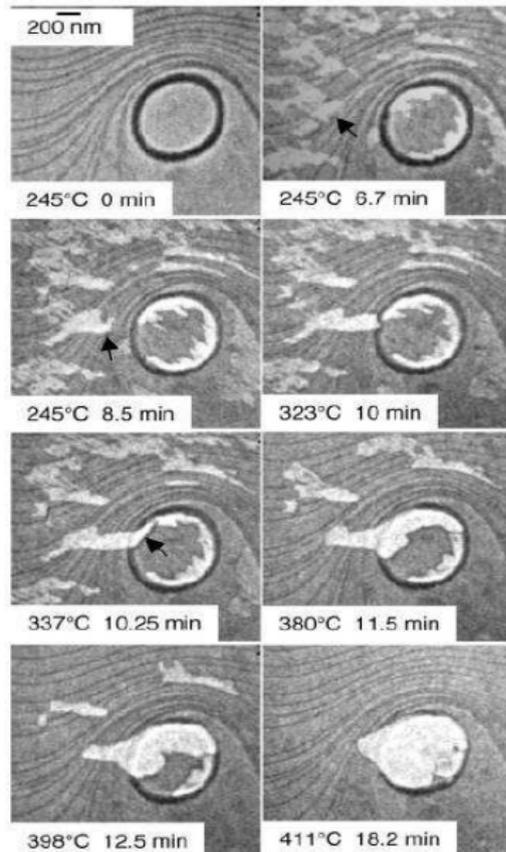
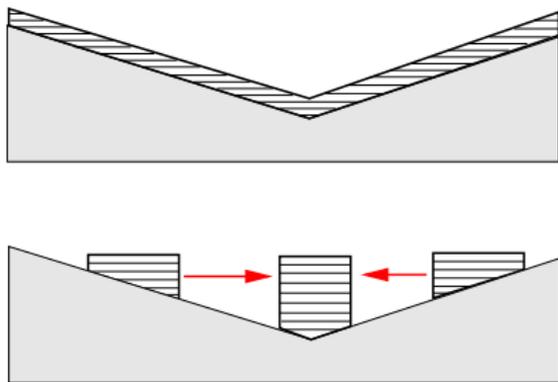
$$E = \gamma_{step} 2\pi\rho - \frac{\gamma_{rough}}{R} \pi\rho^2$$

$$E_b = \pi \frac{\gamma_{step}^2}{\gamma_{surf}} R$$

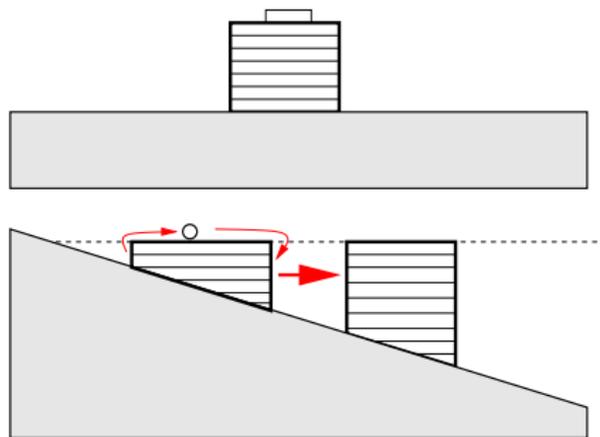
Slow relaxation time  $t \sim e^{E_b/k_B T}$ 

## Experiments

Controlled positioning of mass in holes  
 Ling *et al* Surf. Sci 2006  
 McCarty NanoLetters 2006 Ag/W(110)

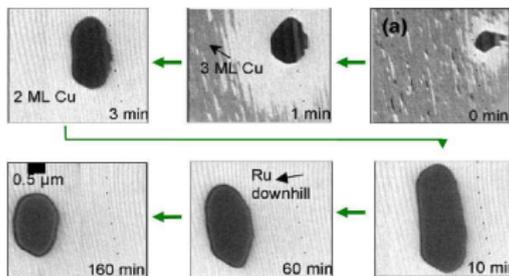


## Nucleationless motion



Going back to equilibrium height  
without nucleation on top??

## De-wetting on a vicinal surface



W. L. Ling et al. Surf. Sci. Lett. (2004)

# Model

$$\mathcal{X} = (x_U + x_D)/2, \text{ and } \mathcal{H} = \mathcal{X} \tan(\theta)$$

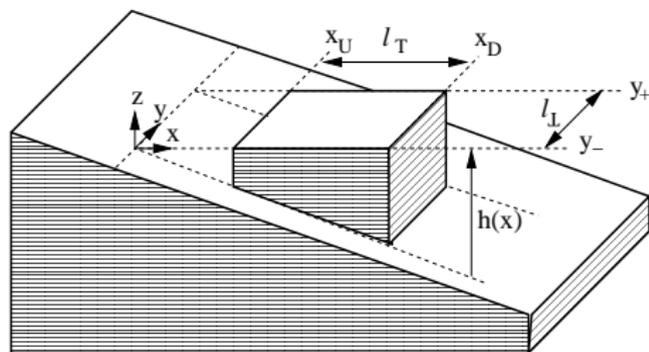
$$l_T = x_U - x_D, \quad l_{\perp} = y_+ - y_-$$

## Einstein-like relation

$$\partial_t \mathcal{X} = -\frac{D_C}{k_B T} \partial_{\mathcal{X}} E_T.$$

## Diffusion limited dynamics

$$D_C \approx \frac{\Omega^2 D_{ceq}}{\mathcal{H}^2 l_T l_{\perp}}$$



Khare, Bartelt, Einstein, Phys. Rev. Lett. 1998

OPL, T.L. Einstein, Phys. Rev.B 2000

# Interfacial and Wetting energies

## Free energy

$$E_l \approx \gamma(h_U + h_D)(l_\perp + l_T) + 2\gamma(1 - \chi)l_T l_\perp$$

$$\chi \gg l_T$$

Maximum aspect ratio  $r = l_\perp / l_T$

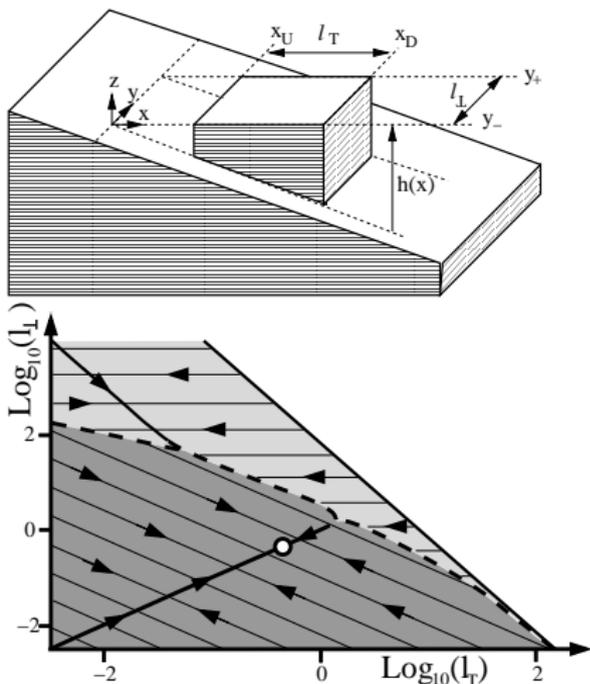
$$r_{max}^l \approx \left( \frac{1 - \chi}{\tan \theta} \right)^{1/4} r_{init}^{3/2}$$

## Drift dynamics

$$\partial_t \chi = \frac{\Omega^2 D c_{eq}}{k_B T} \frac{2\gamma(1 - \chi)}{\chi^3 \tan^2(\theta)}$$

leading to  $\chi \sim t^{1/4}$

(also wetting potential  $\mathcal{W}(h)$ )



## Elastic energy

Exp: Tersoff Tromp, 1993 Ag/Si(100)

Exp: Xu et al 2007, Ge/Si(111)

$$E_E \approx \frac{1}{2} \int dr_j \int dr_k G_{j,k}(\mathbf{r}_j - \mathbf{r}_k) \mathbf{f}_j(\mathbf{r}) \mathbf{f}_k(\mathbf{r})$$

Maximum aspect ratio  $r = l_{\perp} / l_T$ 

$$r_{max}^E = C \frac{V^{1/2}}{\tan(\theta)^{1/2} d_0^{3/2}} e^{-3(3+\sigma)/8(1-\sigma)}$$

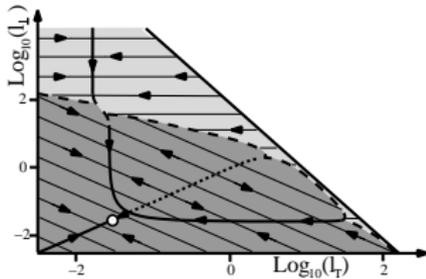
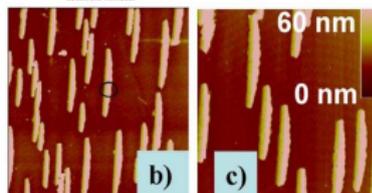
where  $C = 0.175\dots$ 

Drift dynamics

$$\partial_t \mathcal{X} = \frac{\Omega^2 D c_{eq}}{k_B T} \frac{\alpha^2 (1 - \sigma^2)}{\pi Y d_0} e^{-1/(1-\sigma)} \frac{1}{\mathcal{X}}$$

where  $Y$  is the Young modulus.Scaling law  $\mathcal{X} \sim t^{1/2}$ .

FIG. 3. Portion of a Ag island on Si(001), as seen with LEEM. Field of view is 6  $\mu\text{m}$ . Faint wavy lines are steps on substrate surface.



## Other energy

## Metallic layers: Electronic confinement energy

Z. Zhang et al, Phys.Rev.Lett.1998,1999

Metals/Semiconductor

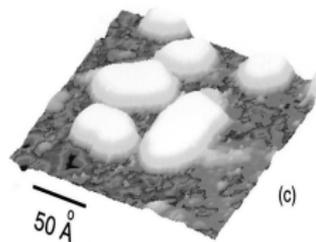
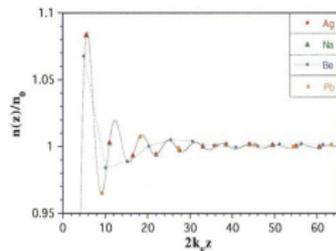
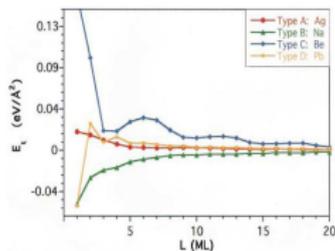
- 1) Quantum confinement of electrons
- 2) Charge spilling in the substrate
- 3) Friedel oscillations

## Van der Waals forces

$$U_{VdW} = -\frac{A}{12\pi h^2}$$

A can be either  $> 0$  or  $< 0$  ???  $A \sim 10^{-20}$  J

Z. Suo and Z. Zhang, Phys Rev B (1998)



Magic thicknesses (as in metal clusters)

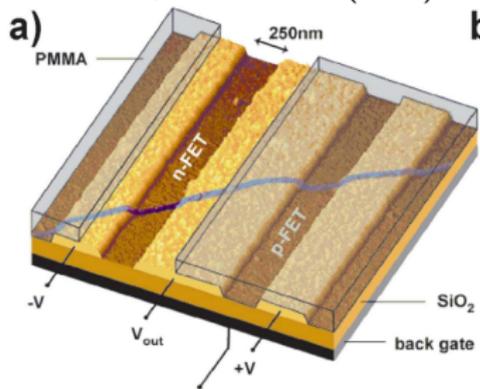
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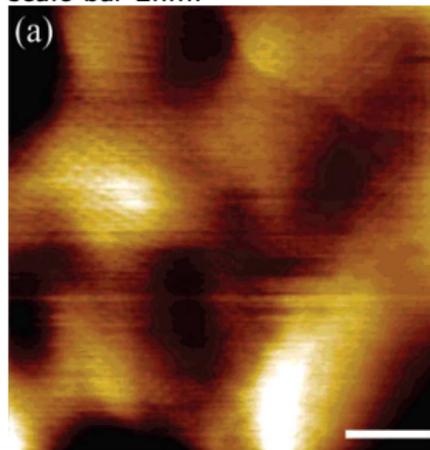
## Carbon nanostructures

Nanotubes on ripples (or grids)  
Derike *et al*, NanoLetters (2001).

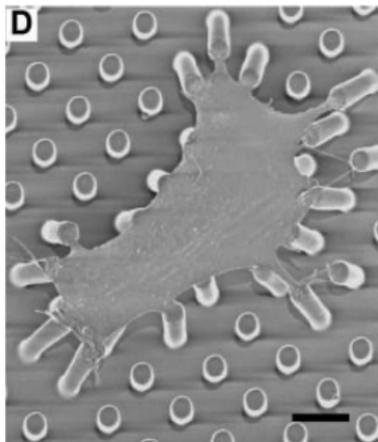


Graphene on rough SiO<sub>2</sub>

E.D. Williams *et al*, NanoLetters (2007);  
scale-bar 2nm.

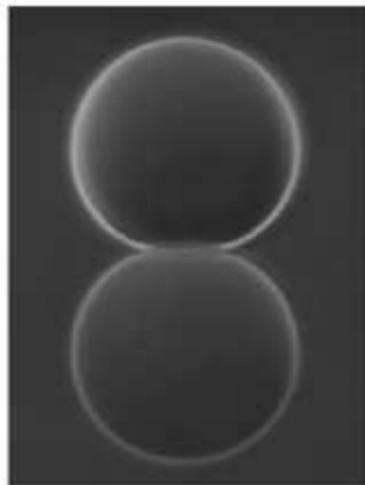


## Lipidic membranes



L. Tan *et al* PNAS (2003); scale-bar  $10\mu\text{m}$

Simple (fluid) lipid membrane on a non-flat surface



M. Abkarian A. Viallat, Biophys J. (2005);  $D = 130\mu\text{m}$

## 1D model: Filament or membrane on ripples



Fakir Carpet



Crenellated



Sinusoidal



Saw tooth

Wavelength  $\lambda$   
Amplitude  $\epsilon$

## Total energy

$$\mathcal{E} = \int ds \left[ \frac{C}{2} \kappa(s)^2 + \sigma + V(\mathbf{r}(s)) \right]$$

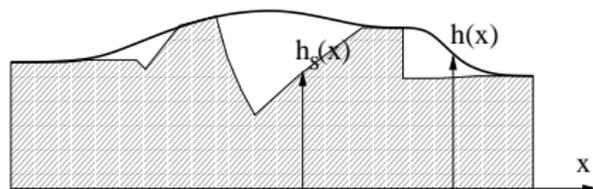
outside solid  $V = 0$ , surface  $V = -\gamma$ ,  
inside  $V = +\infty$ .

i.e. Deformations  $\gg \ell_{eq}$

Adhesion energy  $\gamma$

Bending rigidity  $C$

Tension  $\sigma$



# Equilibrium equations for the Euler elastica with adhesion

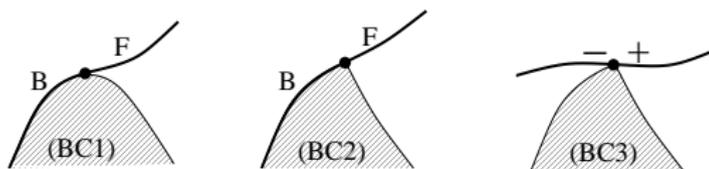
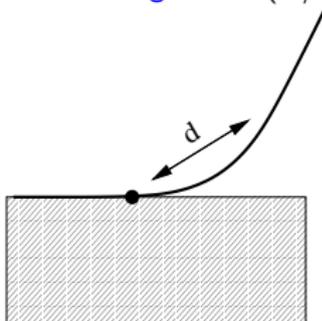


Free parts

$$C \partial_{ss} \kappa + \frac{C}{2} \kappa^3 - \sigma \kappa = 0.$$

Euler-Bernoulli elastica model

Cut-off length  $d = (C/\sigma)^{1/2}$



Boundary conditions

BC1

$$\kappa_F = \kappa_B - \kappa_{eq},$$

where  $\kappa_{eq} = (2\gamma/C)^{1/2}$

BC2

$$\kappa_B - \kappa_{eq} \leq \kappa_F \leq \kappa_B + \kappa_{eq}.$$

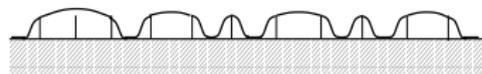
Similar to the Gibbs Inequality Condition for the wetting contact angle

BC3

$$\kappa_+ = \kappa_-, \quad \text{and} \quad \partial_s \kappa_+ \leq \partial_s \kappa_-,$$

# Patterned substrates: a 1D model

## Constructing solutions from $n$ -bridges



All possible solutions

Non-overlapping reduces the number of possible states

## Natural parameters

$$\beta = \frac{\lambda}{d}$$

$\beta \gg 1$  tension dominates

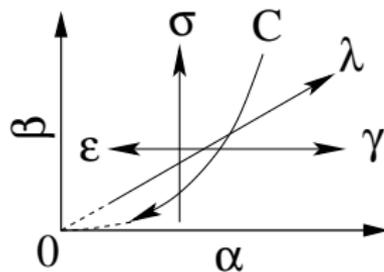
$\beta \ll 1$  curvature dominates

$$\alpha = \left( \frac{\kappa_{eq}}{\kappa_g} \right)^{1/2}$$

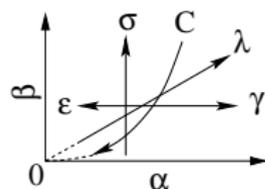
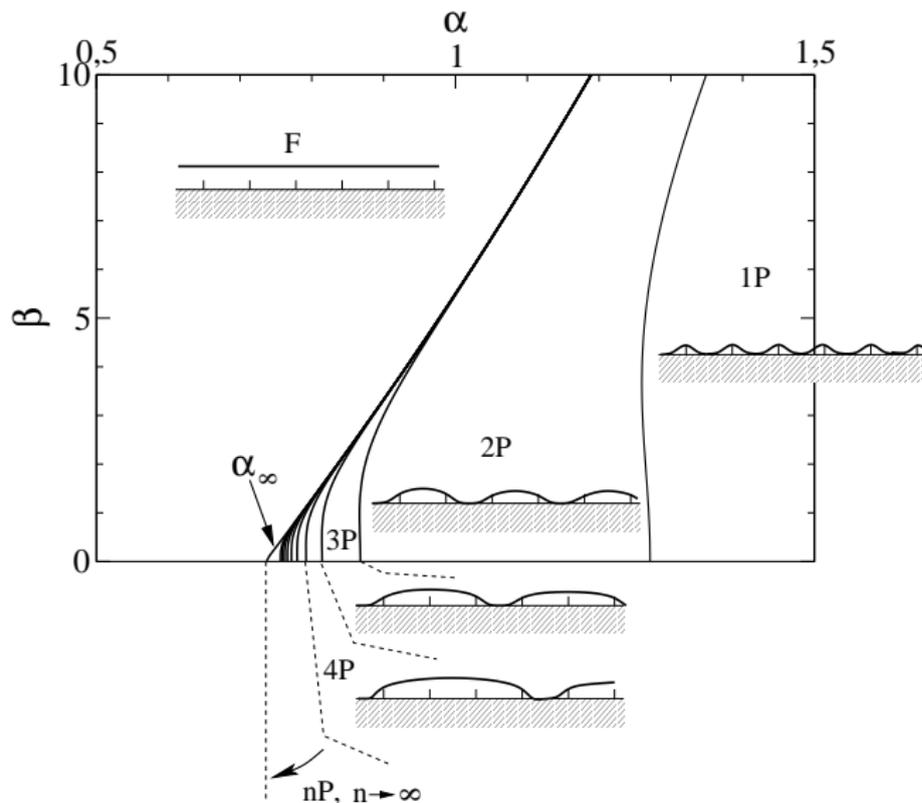
geometrical curvature  $\kappa_g = 4\pi^2\epsilon/\lambda^2$

$\alpha \ll 1 \rightarrow$  Floating state

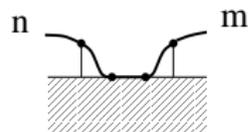
$\alpha \gg 1 \rightarrow$  Membrane follows patterns



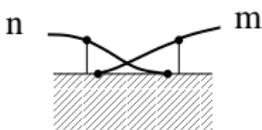
## Ground state Transitions



# Metastability



$$\alpha > \alpha_{n|m}[\beta]$$



$$\alpha < \alpha_{n|m}[\beta]$$

$$\alpha_{n|m}[\beta] > \alpha_{n|m+1}[\beta]$$

$$\alpha_{n|m}[\beta] = \alpha_{m|n}[\beta]$$

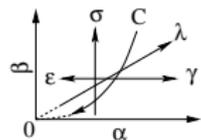
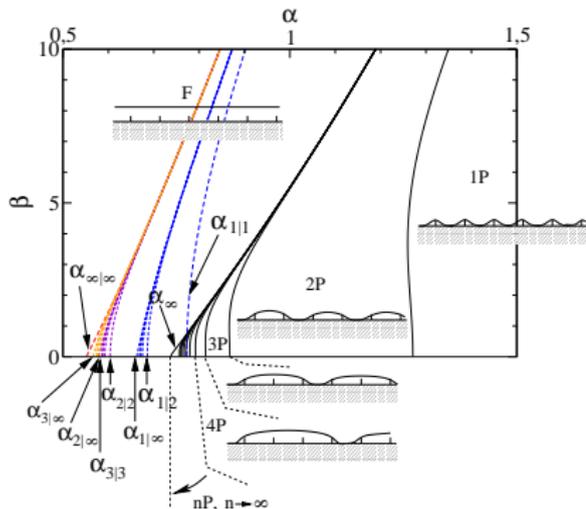
$$\rightarrow \alpha_{n|m}[\beta] > \alpha_{n|m+p}[\beta]$$

But no "total order",

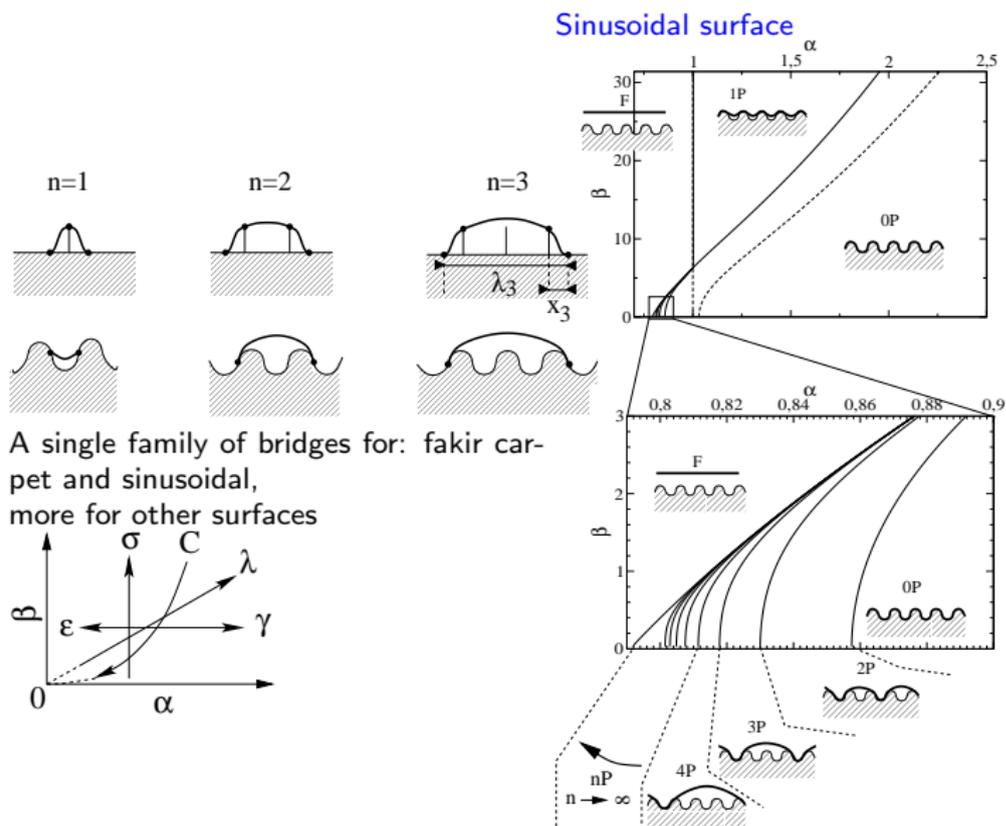
$$\text{e.g. } \alpha_{5|5}[0] < \alpha_{4|9}[0], \text{ and } \alpha_{5|5}[1] > \alpha_{4|9}[1]$$

$\rightarrow$   $\beta$ -dependent decimation order

Non-sticky F ground state at  $\alpha < \alpha_{\infty|\infty}[\beta]$



## Sinusoidal surfaces



# Orders of magnitude

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### Graphene

$$C = 0.9\text{eV}, \gamma \sim 6\text{meV}\text{\AA}^{-2}, \sigma \approx 0$$

$$\rightarrow \epsilon\kappa_{eq} \sim 1.$$

$\epsilon = 1\text{nm}$ , and  $\lambda = 10\text{nm}$ ,  $\Rightarrow \alpha \sim 2$   
larger than  $100\text{nm}$  follow

A. Incze, A. Pasturel and P. Peyla, Phys.Rev.B (2004)

### Oxygen adsorption tunes bending rigidity:

12.5% oxygen  $C = 40\text{eV}$  Peyla et al

$$\epsilon\kappa_{eq} < 1.$$

$$\epsilon = 1\text{nm}, \text{ and } \lambda = 10\text{nm}, \Rightarrow \alpha \approx 0.6.$$

Oxygen adsorption  $\Rightarrow$  scan transition region

## Orders of magnitude

lipid membranes (Swain and Andelman)

$$C = 1.4 \times 10^{-19}\text{J}, \text{ and } \sigma = 1.7 \times 10^{-5}\text{Jm}^{-2}$$

$$\gamma = 5 \times 10^{-6}\text{Jm}^{-2}, \ell_{eq} = 3\text{nm}$$

Choosing

$$\epsilon \approx 50\text{nm} \gg \ell_{eq}, \lambda \approx 500\text{nm} \gg \epsilon,$$

we obtain

$$\Rightarrow \alpha \approx 1.5 \text{ and } \beta \approx 5$$

### Nanotubes

$$\sigma \approx 0, C = 20\text{eV}\cdot\text{nm}, \text{ and } \gamma \approx 1\text{eV}\cdot\text{nm}^{-1}$$

Choosing

$$\epsilon = 5\text{nm}, \lambda = 50\text{nm}$$

we obtain

$$\alpha \approx 2$$

(Nevertheless  $\epsilon\kappa_{eq} \sim 1$ )

# Wetting of solid clusters on nano-patterned surfaces,

How geometry couples to physics

- 1 Liquid drops
- 2 Solid clusters
- 3 Membranes and Filaments
- 4 Conclusion**

# Summary

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R. J. Vrancken, H. Kusumaatmaja, K. Hermans, A.M. Prenten, OPL, C. W. M. Bastiaansen, D.J. Broer, preprint

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- **Membranes and filaments on patterns**

OPL, Phys. Rev. E 2007

# Perspectives

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*OPL, A. Chame, Y. Saito, Phys. Rev. Lett. 2007*

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*OPL, A. Chame, Y. Saito, Phys. Rev. Lett. 2007*
- Nonlinear dynamics, instabilities, and fluctuations of extended fronts  
*OPL, Europhys. Lett. 2005; C. Misbah, OPL, Y. Saito, Rev. Mod. Phys. 2009*

## Elastica: variation of the energy

$s < s_B$  free

$s > s_B$  adhesion

$$\mathcal{E} = \int^{s_B} ds \left[ \frac{C}{2} \kappa^2 + \sigma \right] + \int_{s_B} ds \left[ \frac{C}{2} \kappa^2 + \sigma - \gamma \right].$$

$$\mathbf{t}_{s_B^-} = \mathbf{t}_{s_B^+},$$

**Variation**  $\delta \mathbf{r}(s)$

with  $\delta \mathbf{r}(s) = 0$  for  $s > s_B$ .

$$\begin{aligned} \delta \mathcal{E} &= \int^{s_B} ds (\delta \mathbf{r} \cdot \mathbf{n}) \left[ C \partial_{ss} \kappa + \frac{C}{2} \kappa^3 - \sigma \kappa \right] \\ &+ [ -(\delta \mathbf{r} \cdot \mathbf{n}) C \partial_s \kappa + (\partial_s \delta \mathbf{r} \cdot \mathbf{n}) C \kappa ] \Big|_{s_B^-} \\ &+ ds_B \left[ \left( \frac{C}{2} \kappa^2 + \sigma \right) \Big|_{s_B^-} - \left( \frac{C}{2} \kappa^2 + \sigma - \gamma \right) \Big|_{s_B^+} \right] \end{aligned}$$